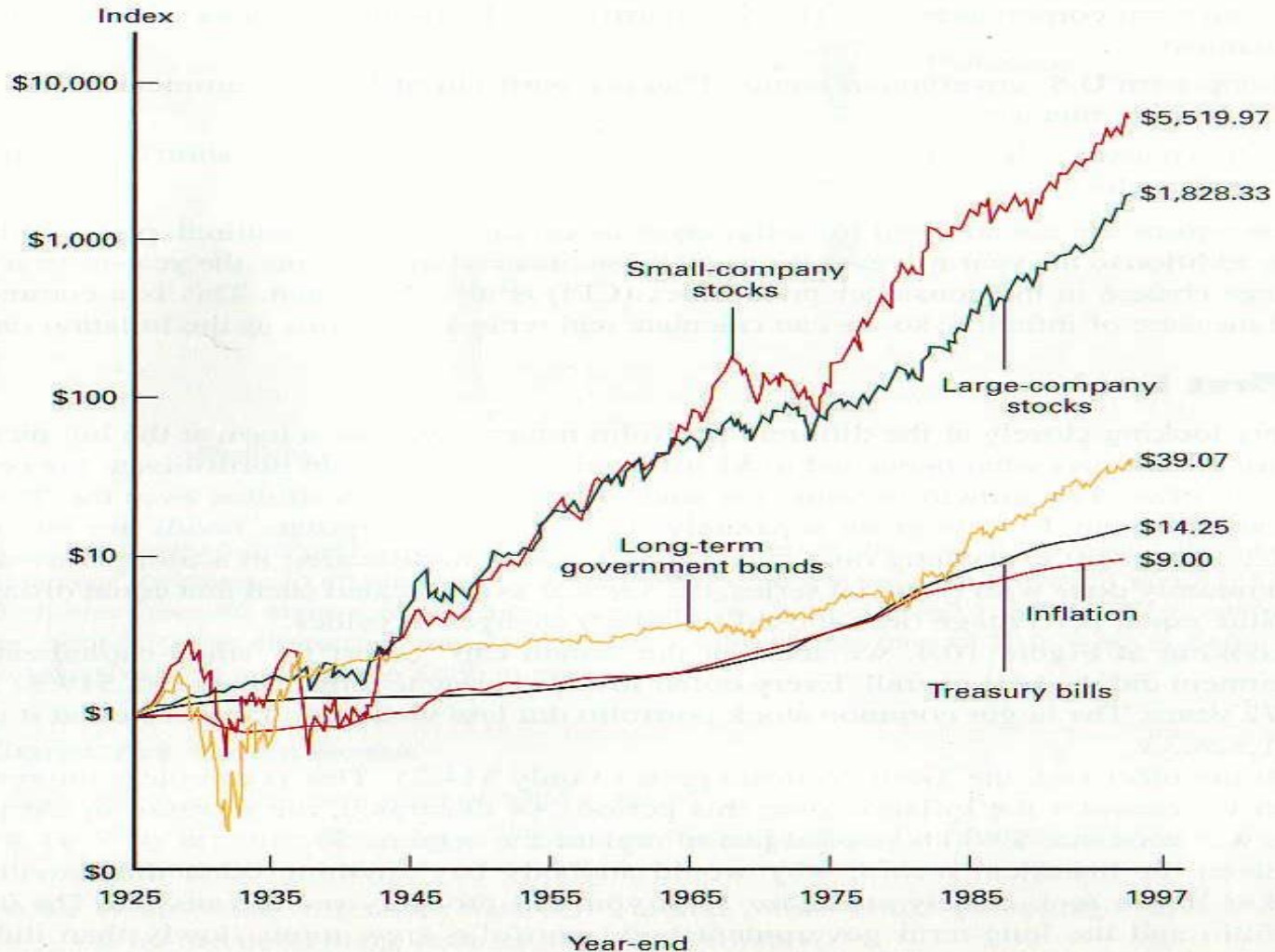


# Risk and Return

- 1. What rate of return do you expect on your investment (savings) this year?**
- 2. What rate will you actually earn?**
- 3. Does it matter if it is a bank FD or a share of a mobile VAS player (say, Onmobile India)?**

# A \$1 Investment in different types of portfolios: 1926-1997 (Year end 1925 = \$1)



SOURCE: *Stocks, Bonds, Bills, and Inflation 1997 Yearbook™*, Ibbotson Associates, Inc., Chicago (annually updates work by Roger G. Ibbotson and Rex A. Sinquefeld). All rights reserved.

# Annual Average Returns 1926-1997

Investment	Average Return
Common stocks	13.0%
Small stocks	17.7
Long-term corporate bonds	6.1
Long-term government bonds	5.6
U.S. Treasury bills	3.8
Inflation	3.2

SOURCE: *Stocks, Bonds, Bills, and Inflation 1997 Yearbook™*, Ibbotson Associates, Inc., Chicago (annually updates work by Roger G. Ibbotson and Rex A. Sinquefeld). All rights reserved.

## Annual Average Returns in India

- Large Cap Shares (say, Sensex) 1 → 137  
(28 years, 1979-2007)
- Bank Fixed Deposits (say, 5-year) 1 → 14  
(28 years, 1979-2007)
- But, try looking at the yearly rates of return in each of the cases
- The most fluctuating will be stocks i.e., stock returns vary widely over time.

# Introduction

- **Unfortunately, if we try for future, the graph is expected risk and return (a.k.a. security market line)**
- **Investors demand for more from a riskier project**
- **Unfortunately, it is (really) difficult -- if not impossible -- to make such predictions with any degree of certainty.**
- **As a result, investors often use history as a basis for predicting the future.**
- **We will begin by evaluating the risk and return characteristics of individual assets, and end by looking at portfolios of assets.**
- **How do we find the risk of an individual asset (say, a equity share)**

# Risk and Return Defined

- In the context of business and finance, risk is defined as the chance of suffering a financial loss.
- Assets (real or financial) which have a greater chance of loss are considered more risky than those with a lower chance of loss.
- Risk may be used interchangeably with the term uncertainty to refer to the variability of returns associated with a given asset.
- Return represents the total gain or loss on an investment

# Example

<b>Risk and Return</b>		
	<b><u>Return</u></b>	
<b><u>year</u></b>	<b><u>Stock A</u></b>	<b><u>Stock B</u></b>
1	6%	20%
2	12%	30%
3	8%	10%
4	-2%	-10%
5	18%	50%
6	6%	20%



# Single Financial Assets

## Historical Risk

### Standard Deviation

year	Observed Return for Stock A	Observed Return for Stock B	year	Observed Return for Stock A	Observed Return for Stock B
1	0.06	0.2	1	6%	20%
2	0.12	0.3	2	12%	30%
3	0.08	0.1	3	8%	10%
4			4		0%
5			5		0%
6	0.06	0.2	6		20%
<b>Average</b>	<b>=AVERAGE(B4:B9)</b>	<b>=AVERAGE(C4:C9)</b>	<b>Average</b>	<b>8.00%</b>	<b>20.00%</b>
<b>Standard Deviation</b>	<b>=STDEV(B4:B9)</b>	<b>=STDEV(C4:C9)</b>	<b>Standard Deviation</b>	<b>6.69%</b>	<b>20.00%</b>

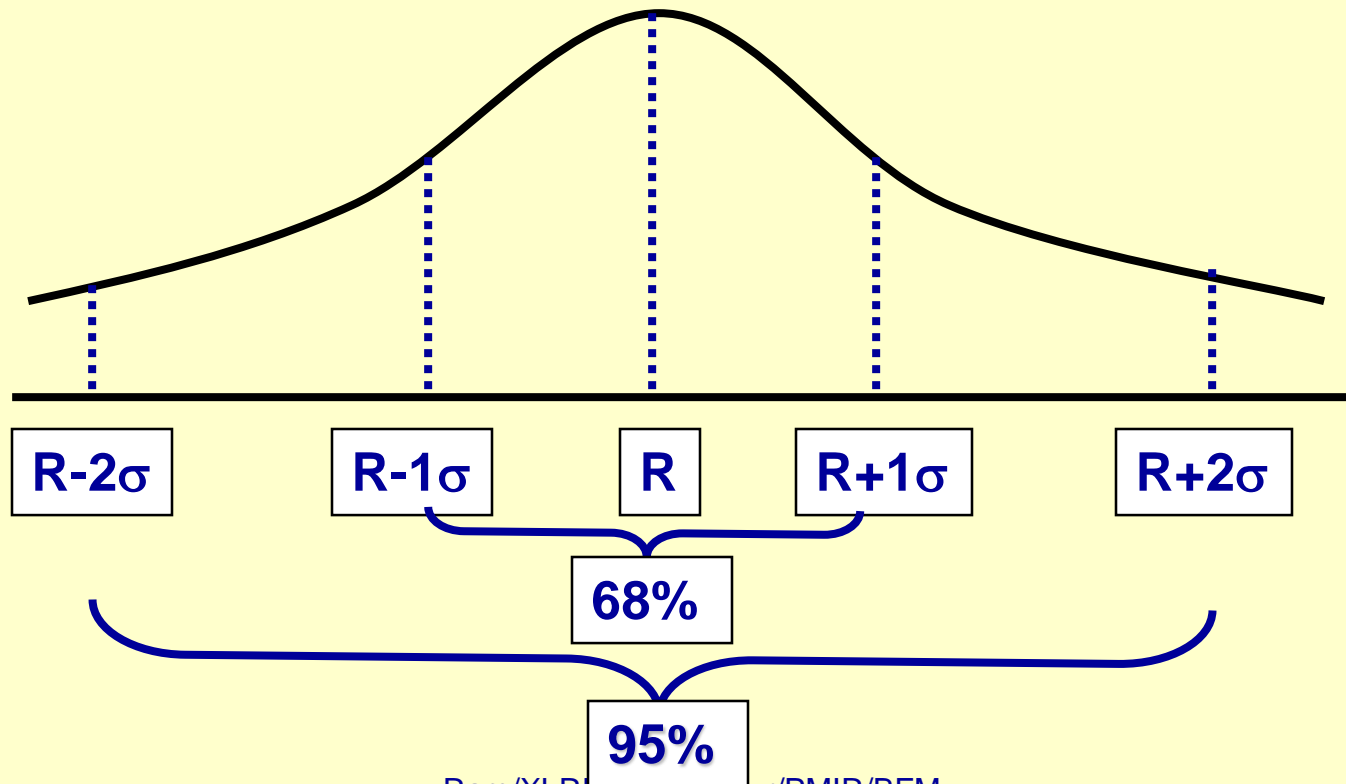
**What you type**

**What you see**

# Single Financial Assets

## Historical Risk

### Normal Distribution



# Single Financial Assets

## Expected Return & Risk

- Investors and analysts often look at historical returns as a starting point for predicting the future.
- However, they are much more interested in what the returns on their investments will be in the future.
- For this reason, we need a method for estimating future or “ex-ante” returns.
- One way of doing this is to assign probabilities for future states of nature and the returns that would be realized if a particular state of nature would occur.

# Single Financial Assets

## Expected Return & Risk

Expected Return  $E(R) = \sum p_i R_i$ ,

where  $p_i$  = probability of the  $i$ th scenario, and

$R_i$  = the forecasted return in the  $i$ th scenario.

Also, the variance of  $E(R)$  may be computed as:

$$\sigma^2 = \sum p_i [R_i - E(R)]^2$$

and hence the standard deviation as:

$$\sqrt{\sigma^2} = \sqrt{\sum p_i [R_i - E(R)]^2}$$

# Single Financial Assets

## Expected Return & Risk

Expected Return			
State	Probability	Stock A	Stock B
Boom	30%	17%	29%
Normal	50%	12%	15%
Bust	20%	5%	-2%
Expected Return		12.1%	15.8%

# Single Financial Assets

## Expected Return & Risk

Risk, Variance, & Standard Deviation			
State	Pi	Stock A	$pi[A_i - E(R)]^2$
Boom	0.30	17	7.203
Normal	0.50	12	0.005
Bust	0.20	5	10.082
Expected Return		12	
Variance = Sum of $pi[A_i - E(R)]^2$			17.290
Standard Deviation = $(Var)^{1/2}$			4.158

# Single Financial Assets

## Coefficient of Variation

- One problem with using standard deviation as a measure of risk is that we cannot easily make risk comparisons between two assets.
- The coefficient of variation overcomes this problem by measuring the amount of risk per unit of return.
- The higher the coefficient of variation then more is the risk per return.
- So, an investor would prefer selecting the asset with the lower coefficient of variation.

# Single Financial Assets

## Coefficient of Variation

<b>Coefficient of Variation</b>			
<b>State</b>	<b>Pi</b>	<b>Stock A</b>	<b>Stock B</b>
<b>Boom</b>	<b>0.3</b>	<b>17</b>	<b>30</b>
<b>Normal</b>	<b>0.5</b>	<b>12</b>	<b>15</b>
<b>Bust</b>	<b>0.2</b>	<b>5</b>	<b>-5</b>
<b>Expected Return</b>		<b>12.1</b>	<b>15.5</b>
<b>Standard Deviation</b>		<b>4.16</b>	<b>10.517</b>
<b>Coefficient of Variation</b>		<b>0.344</b>	<b>0.679</b>



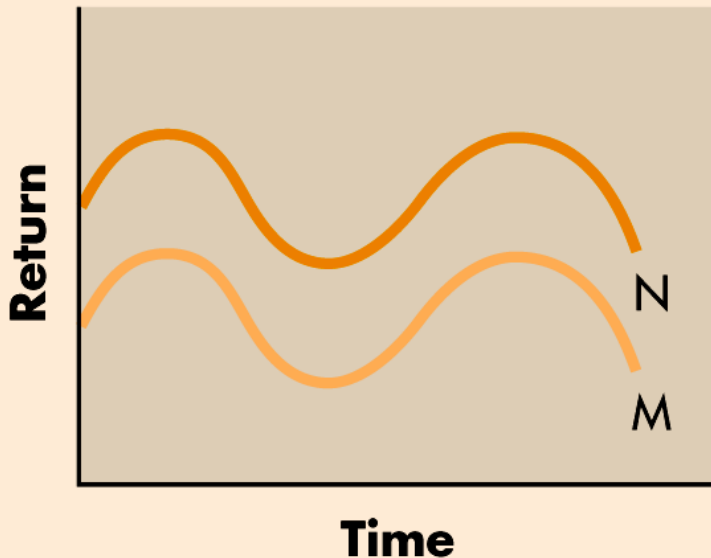
# Portfolios of Assets

- An investment portfolio is any collection or combination of financial assets.
- If we assume all investors are rational and therefore risk averse, that investor will ALWAYS choose to invest in portfolios rather than in single assets.
- Investors will hold portfolios because he or she will *diversify* away a portion of the risk
- If an investor holds a single asset, he or she will fully suffer the consequences of poor performance.

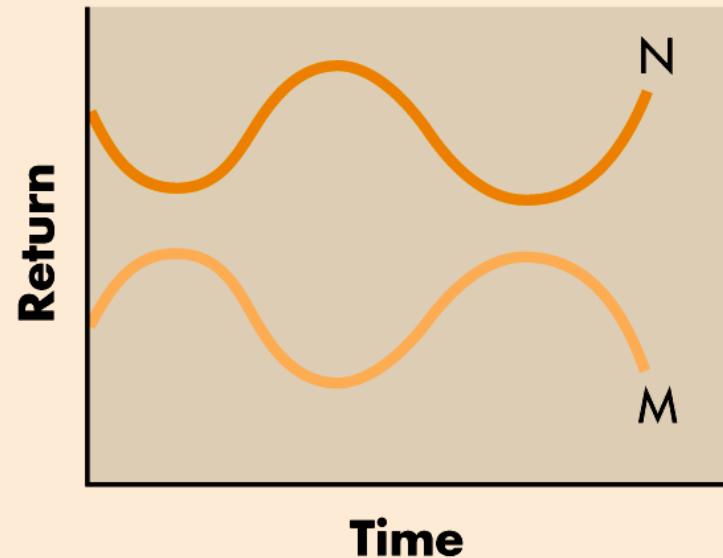
# Portfolios of Assets

- Diversification is enhanced depending upon the extent to which the returns on assets “move” together.
- This movement is typically measured by a statistic known as “correlation” as shown in Figures below

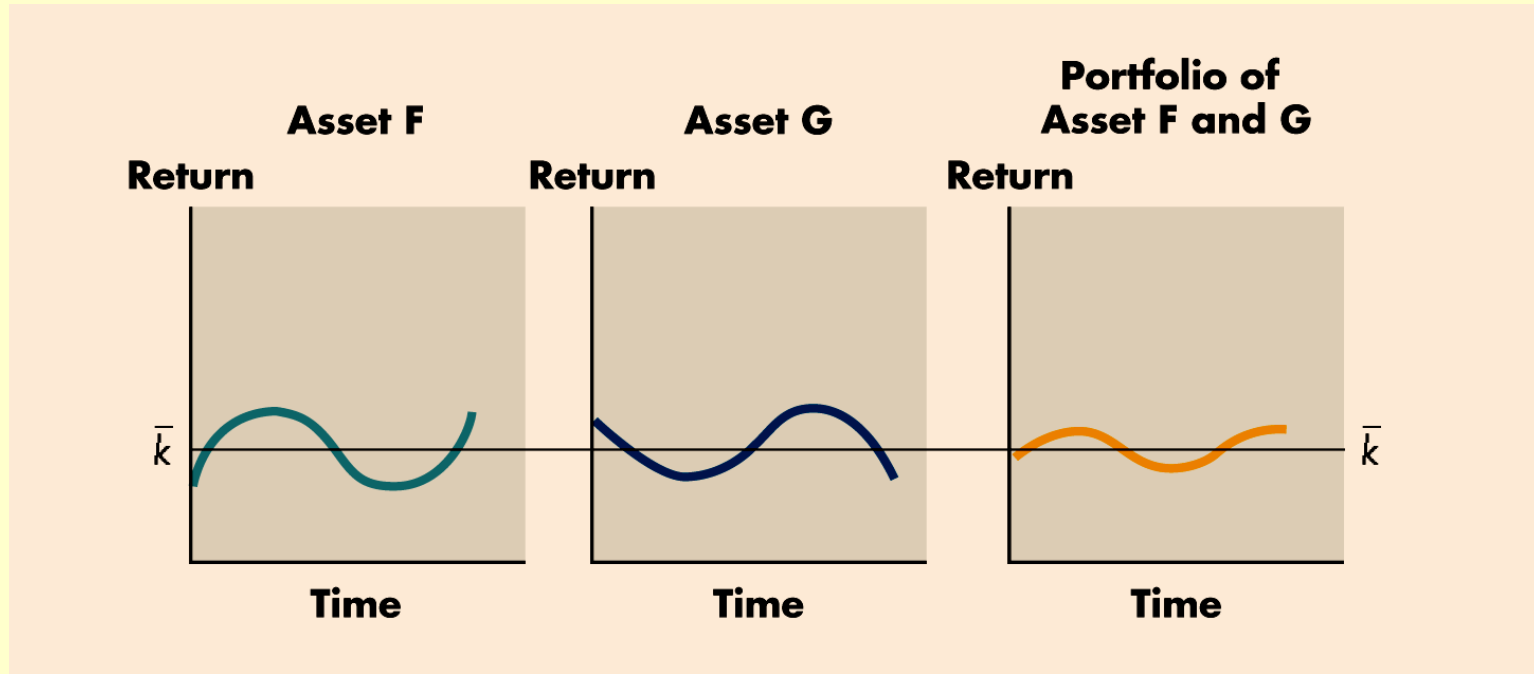
**Perfectly Positively Correlated**



**Perfectly Negatively Correlated**



# Portfolios of Assets



# Portfolios of Assets

## Portfolio AB

(50% in A, 50% in B)

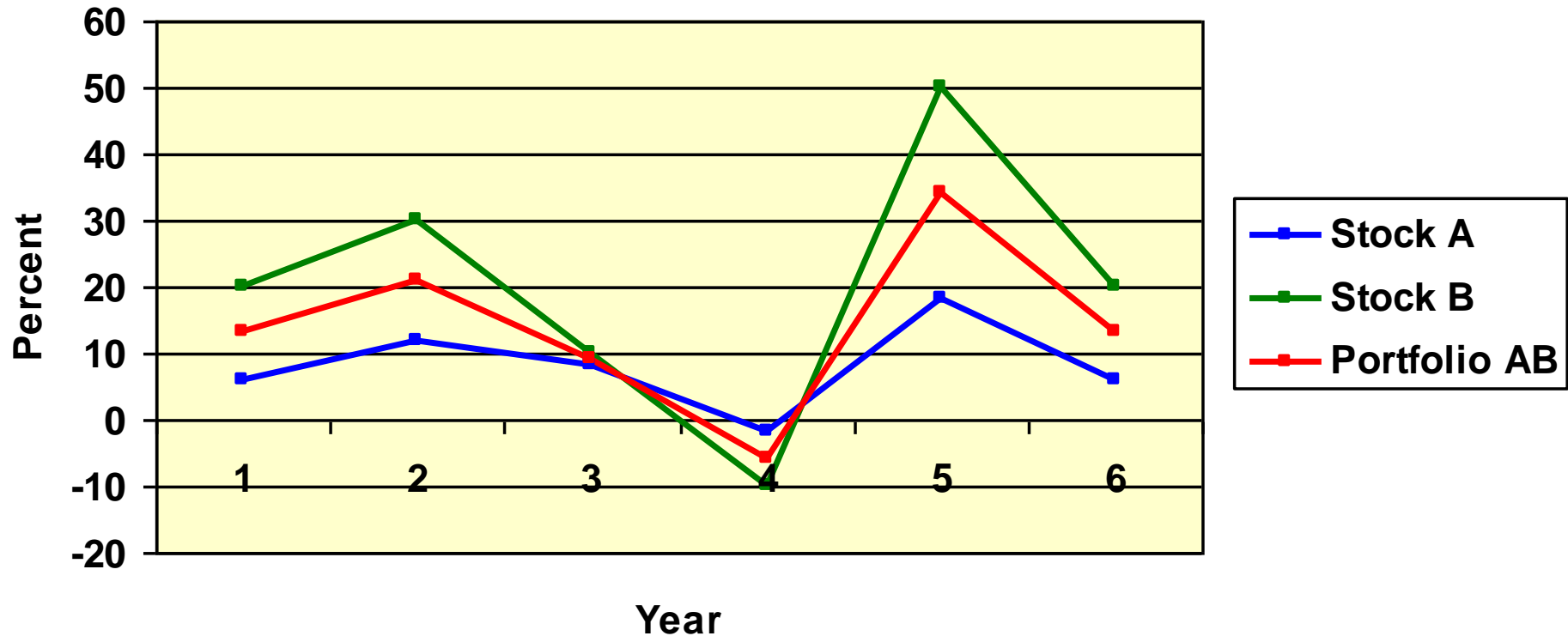
Year	Stock A		Stock B		Portfolio AB
	Percent Weight	Percent Return	Percent Weight	Percent Return	Weighted Return
1	50%	6	50%	20	13
2	50%	12	50%	30	21
3	50%	8	50%	10	9
4	50%	-2	50%	-10	-6
5	50%	18	50%	50	34
6	50%	6	50%	20	13
<b>Weight A</b>	<b>50%</b>		<b>Sum of Weighted Returns</b>		<b>84</b>
<b>Weight B</b>	<b>50%</b>		<b>Portfolio Average Return</b>		<b>14</b>

# Portfolios of Assets

## Portfolio AB

(50% in A, 50% in B)

### Investment Returns



# Portfolios of Assets

## Portfolio AB

(40% in A, 60% in B)

Year	Stock A		Stock B		Portfolio AB
	Percent Weight	Percent Return	Percent Weight	Percent Return	Weighted Return
1	40%	6	60%	20	14.4
2	40%	12	60%	30	22.8
3	40%	8	60%	10	9.2
4	40%	-2	60%	-10	-6.8
5	40%	18	60%	50	37.2
6	40%	6	60%	20	14.4
<b>Weight A</b>	<b>40%</b>		<b>Sum of Weighted Returns</b>		<b>91.2</b>
<b>Weight B</b>	<b>60%</b>		<b>Portfolio Average Return</b>		<b>15.2</b>

**Changing the weights**

# Portfolios of Assets

## Portfolio AB

(20% in A, 80% in B)

Year	Stock A		Stock B		Portfolio AB
	Percent Weight	Percent Return	Percent Weight	Percent Return	Weighted Return
1	20%	6	80%	20	17.2
2	20%	12	80%	30	26.4
3	20%	8	80%	10	9.6
4	20%	-2	80%	-10	-8.4
5	20%	18	80%	50	43.6
6	20%	6	80%	20	17.2
<b>Weight A</b>	<b>20%</b>		<b>Sum of Weighted Returns</b>		<b>105.6</b>
<b>Weight B</b>	<b>80%</b>		<b>Portfolio Average Return</b>		<b>17.6</b>

And Again

# Portfolios of Assets

## Portfolio Risk & Return

Summarizing changes in risk and return as the composition of the portfolio changes.

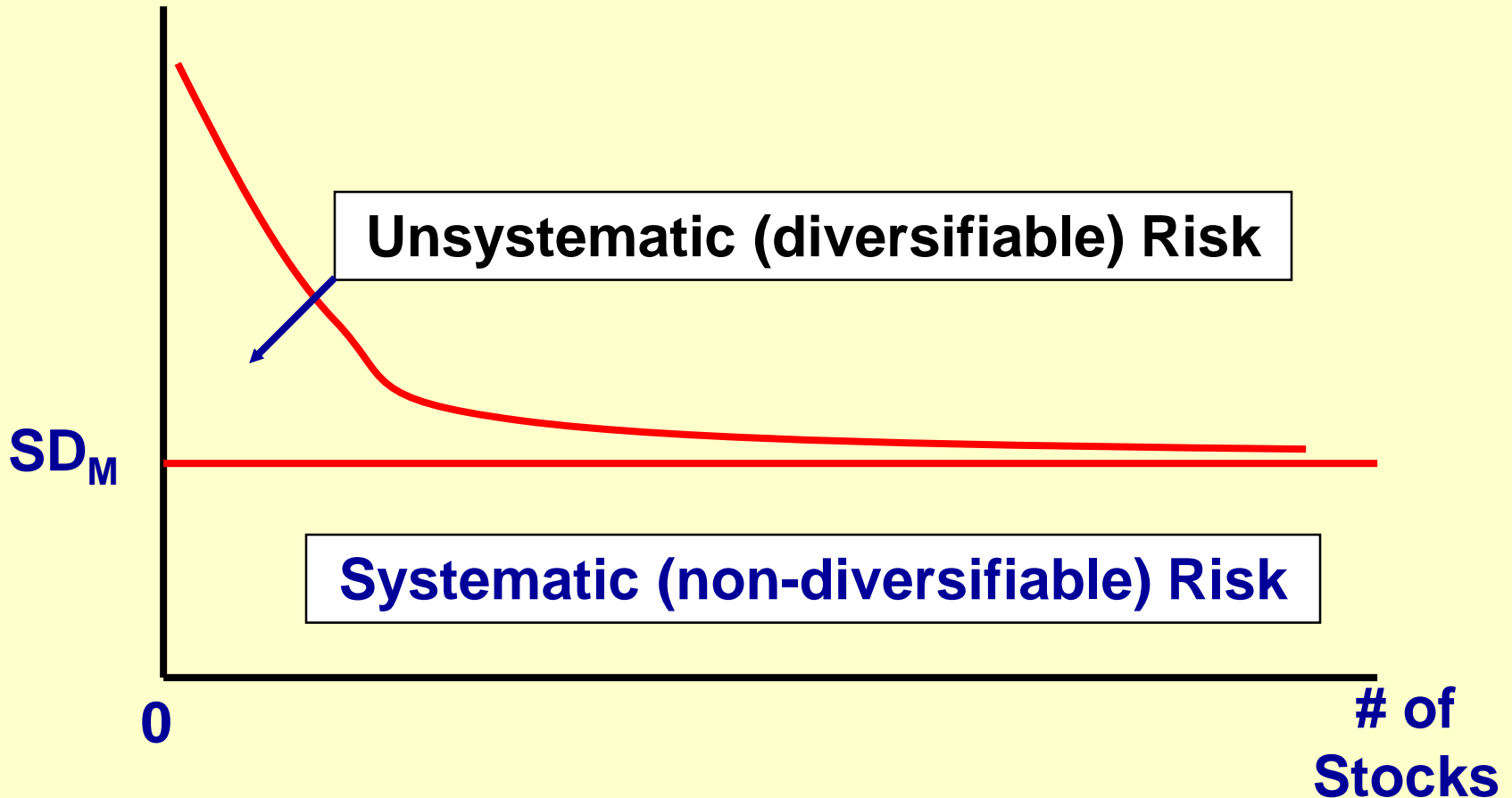
Weight A	Return A (%)	Return B (%)	Return AB (%)	SD-A (%)	SD-B (%)	SD-AB (%)
100%	8.0	20.0	8.0	6.7	20.0	6.7
80%	8.0	20.0	10.4	6.7	20.0	9.3
60%	8.0	20.0	12.8	6.7	20.0	11.9
40%	8.0	20.0	15.2	6.7	20.0	14.6
20%	8.0	20.0	17.6	6.7	20.0	17.3
0%	8.0	20.0	20	6.7	20.0	20.0



# Portfolios of Assets

## Portfolio Risk (Adding Assets to a Portfolio)

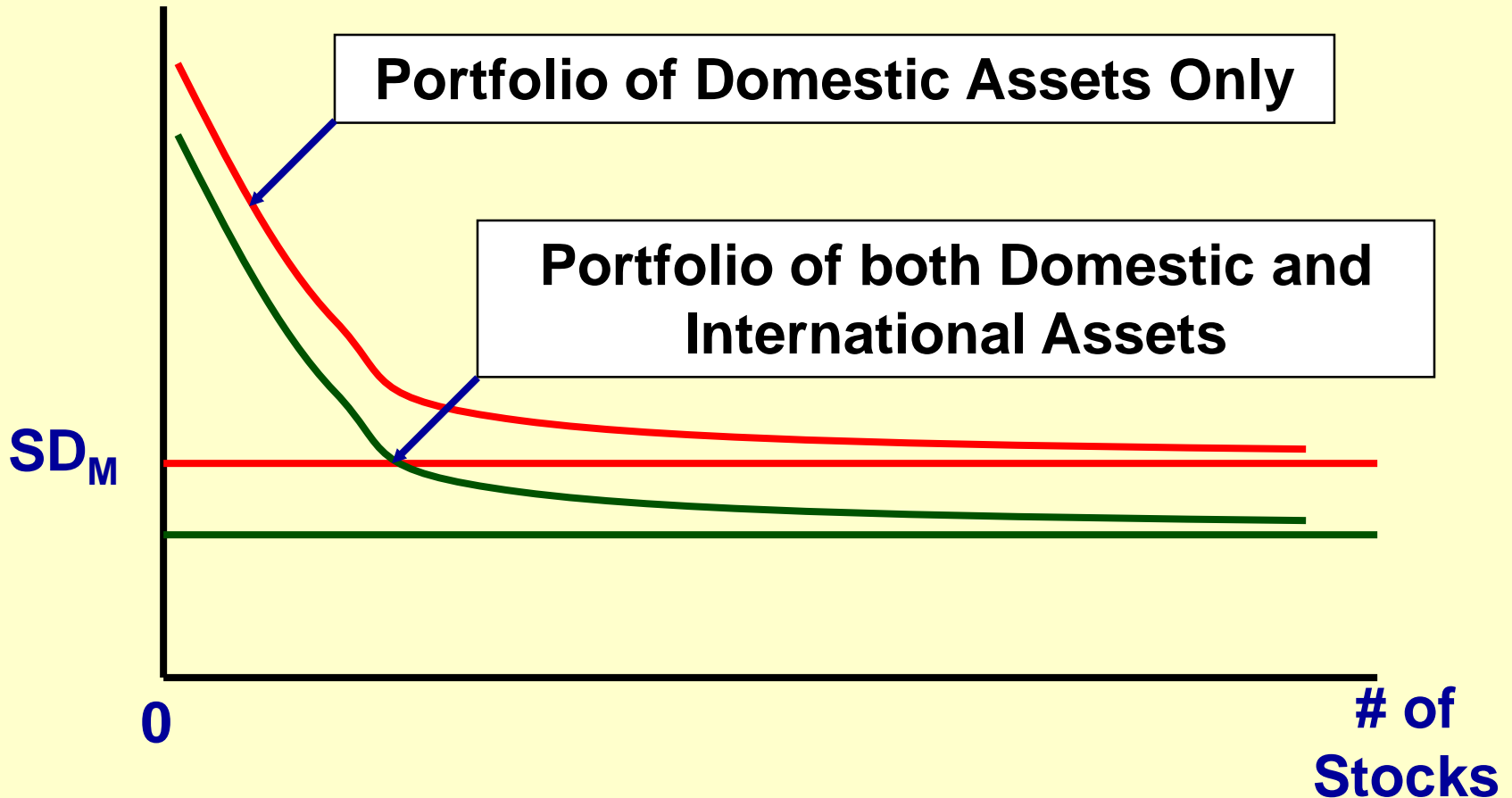
Portfolio Risk (SD)



# Portfolios of Assets

## Portfolio Risk (Adding Assets to a Portfolio)

Portfolio Risk (SD)



# Portfolios of Assets

## Capital Asset Pricing Model (CAPM)

- If you notice, a good part of a portfolio's risk (the standard deviation of returns) can be eliminated simply by holding a lot of stocks.
- The risk you can't get rid of by adding stocks (systematic) cannot be eliminated through diversification because that variability is caused by events that affect most stocks similarly.
- Examples would include changes in macroeconomic factors such interest rates, inflation, and the business cycle.

# Portfolios of Assets

## Capital Asset Pricing Model (CAPM)

- In the early 1960s, Sharpe & co developed an asset pricing model that measures only the amount of systematic risk a particular asset has.
- In other words, they noticed that most stocks go down when interest rates go up, but some go down a whole lot more.
- They reasoned that if they could measure this variability -- the systematic risk -- then they could develop a model to price assets using only this risk.
- The unsystematic (company-related) risk is irrelevant because it could easily be eliminated simply by diversifying.

# Portfolios of Assets

## Capital Asset Pricing Model (CAPM)

- To measure the amount of systematic risk an asset has, they simply regressed the returns for the “market portfolio” -- the portfolio of ALL assets - against the returns for an individual asset.
- The slope of the regression line -- beta -- measures an assets systematic (non-diversifiable) risk.
- In general, cyclical companies like auto companies have high betas while relatively stable companies, like public utilities, have low betas.
- Let's look at an example to see how this works.

# Portfolios of Assets

## Capital Asset Pricing Model (CAPM)

SUMMARY OUTPUT

Regression Statistics

Multiple R 0.993698

**This slide is the result of a regression using the Excel. The slope of the regression (beta) in this case is 1.92. Apparently, this stock has a considerable amount of systematic risk.**

F	Significance F
235.7556	0.0006

Total

2000

	Coefficient	Standard Error	t Stat	P-value	Lower 95%	Upper 95%	Lower 95.0%	Upper 95.0%
Intercept	-3.7751	2.018166	-1.87057	0.158163	-10.1978	2.64758	-10.1978	2.64758
10	1.917349	0.124873	15.35433	0.0006	1.519946	2.314753	1.519946	2.314753

# What is Beta?

An index of **systematic risk**.

It measures the sensitivity of a stock's returns to changes in returns on the market portfolio.

The **beta** for a portfolio is simply a weighted average of the individual stock betas in the portfolio.

# Portfolios of Assets

## Capital Asset Pricing Model (CAPM)

- The **required return** for *all* assets is composed of two parts: the risk-free rate and a risk premium.

The risk premium is a function of both market conditions and the asset itself.

The risk-free rate ( $r_f$ ) is usually estimated from the return on Govt. Treasury bills



# Portfolios of Assets

## Capital Asset Pricing Model (CAPM)

- The **risk premium** for a stock is composed of two parts:
  - The **Market Risk Premium** which is the return required for investing in any risky asset rather than the risk-free rate
  - **Beta**, a risk coefficient which measures the sensitivity of the particular stock's return to changes in market conditions.

# Portfolios of Assets

## Capital Asset Pricing Model (CAPM)

- After estimating beta, which measures a specific asset's systematic risk, it is relatively easy to estimate other variables (may be obtained to calculate an asset's required return) ...

$$K_e = R_f + \beta [R_m - R_f], \text{ where}$$

$K_e$  = an asset's expected or required return,

$R_f$  = the risk free rate of return,

$\beta$  = an asset or portfolio's beta

$R_m$  = the expected return on the market portfolio.

# Portfolios of Assets

## Capital Asset Pricing Model (CAPM)

### Example

Calculate the required return for RIL shares assuming it has a beta of 1.1, the rate on T-bills is 8%, and the expected return for the BSE Sensex is 16%.

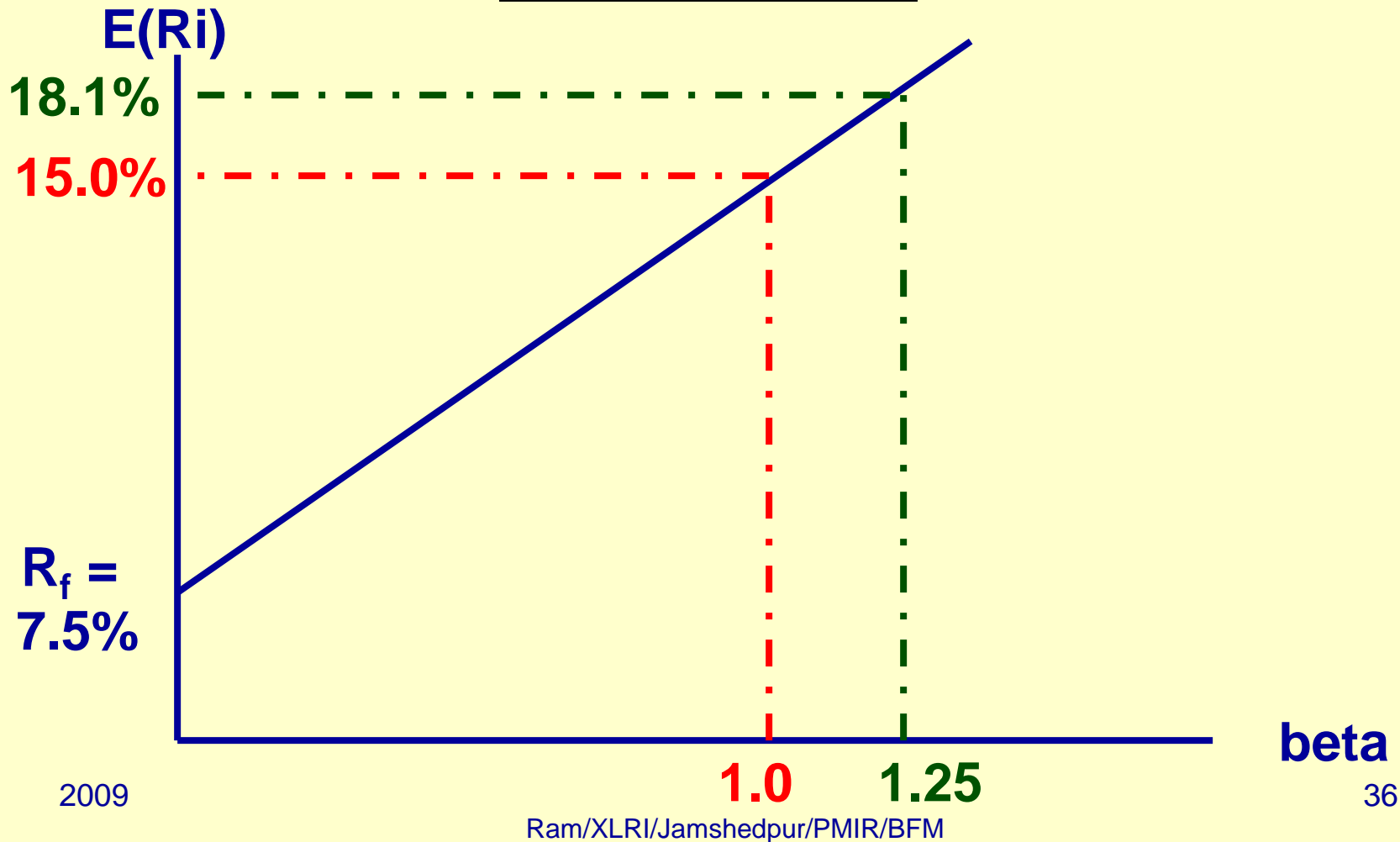
$$K_e = 8 + 1.1 [16\% - 8\%]$$

$$K_e = 16.8\%$$

# Portfolios of Assets

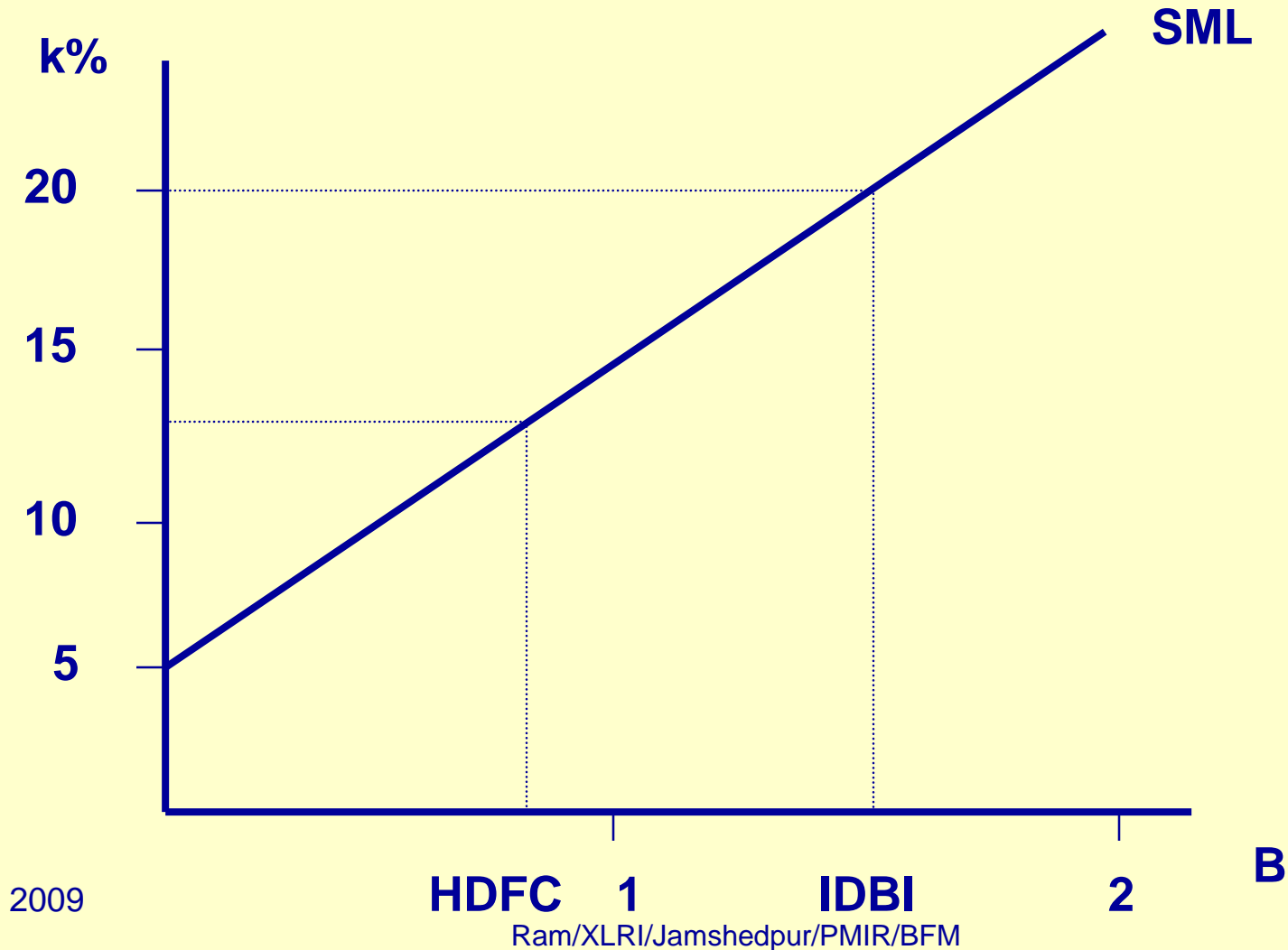
## Capital Asset Pricing Model (CAPM)

Graphically



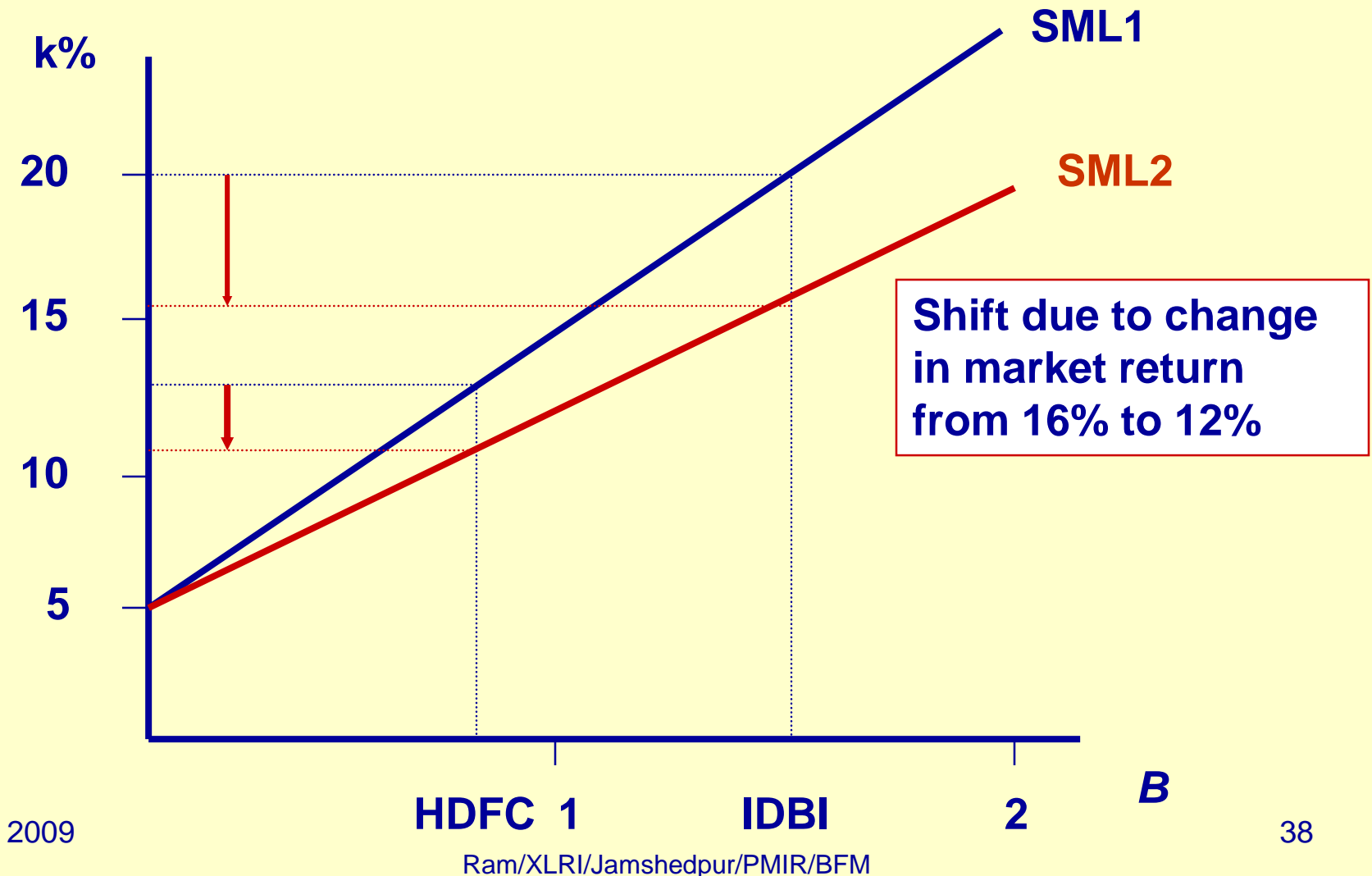
# Portfolios of Assets

## Capital Asset Pricing Model (CAPM)



# Portfolios of Assets

## Capital Asset Pricing Model (CAPM)



# Estimates of Beta for Selected Individual Indian Stocks (Source: NSE India)

Stock	Beta
BPCL	0.66
Grasim	1.14
Hero Honda	0.66
ITC	0.94
Mahindra & Mahindra	1.02
Reliance Industries	1.00
Suzlon Energy	1.25
VSNL	1.44